Self-Scheduling Approach to Coordinating Wind Power Producers with Energy Storage and Demand Response

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Abstract—The uncertainty of wind energy makes wind power producers (WPPs) incur profit loss due to balancing costs in electricity markets, a phenomenon that restricts their participation in markets. This paper proposes a stochastic bidding strategy based on virtual power plants (VPPs) to increase the profit of WPPs in short-term electricity markets in coordination with energy storage systems (ESSs) and demand response (DR). To implement the stochastic solution strategy, the Kantorovich method is used for scenario generation and reduction. The optimization problem is formulated as a Mixed-Integer Linear Programming (MILP) problem. From testing the proposed method for a Spanish WPP, it is inferred that the proposed method enhances the profit of the VPP compared to previous models.

Index Terms—Wind Energy; Energy Storage System; Demand Response; Uncertainty; Stochastic Programming; Electricity Market.

NOMENCLATURE

Indices

\( t (N) \) \hspace{1cm} \text{Timeslot index (number of timeslots).}
\( \omega (N_\omega) \) \hspace{1cm} \text{Scenario index (number of scenarios).}
\( l (N_l) \) \hspace{1cm} \text{Linearized segment index (number of segments).}

Parameters

\( W_{\text{max}} \) \hspace{1cm} \text{Wind unit capacity (MW).}
\( \lambda^D, \lambda^I \) \hspace{1cm} \text{Energy price in the DA and intraday markets, respectively ($/MWh).}
\( \rho_\omega \) \hspace{1cm} \text{Probability of scenario } \omega.
\( R^+, R^- \) \hspace{1cm} \text{Ratio of positive and negative, respectively, energy imbalance of WPP with respect to DA market.}
\( \gamma \) \hspace{1cm} \text{The ratio of WPP offer in the intraday market with respect to the DA market.}
\( \lambda^* \) \hspace{1cm} \text{Payment rate for incentive-based DR ($/MWh).}

Variables

\( P^D, P^I \) \hspace{1cm} \text{WPP offer in the DA and intraday markets, respectively (MW).}
\( P^\text{sch} \) \hspace{1cm} \text{Scheduled power of WPP (MW).}
\( W \) \hspace{1cm} \text{Power output of WPP (MW).}
\( \delta \) \hspace{1cm} \text{Power deviation of WPP from its scheduled value (MW).}
\( \delta^+, \delta^- \) \hspace{1cm} \text{Positive and negative, respectively, power deviation of WPP with respect to scheduled value (MW).}
\( L^D, L^I \) \hspace{1cm} \text{Curtable load offer of DR in DA and intraday markets, respectively (MW).}
\( L^\text{sch} \) \hspace{1cm} \text{Scheduled curtable load of DR (MW).}
\( L^\text{sch,I} \) \hspace{1cm} \text{Linearized segments of } L^\text{sch} (MW). \hspace{1cm}
\( P^\text{ch,D} \) \hspace{1cm} \text{Charging offer of ESS in the DA market (MW).}
\( P^\text{ch,D} \) \hspace{1cm} \text{Discharging offer of ESS in the DA market (MW).}
\( P^\text{ch,I} \) \hspace{1cm} \text{Charging offer of ESS in the intraday market (MW).}
\( P^\text{ch,I} \) \hspace{1cm} \text{Discharging offer of ESS in the intraday market (MW).}
\( y \) \hspace{1cm} \text{Binary variable equal to 1 if the ESS is being charged.}
\( P^{\text{sch}, \text{ch}} \) \hspace{1cm} \text{Scheduled charging offer of ESS (MW).}
\( P^{\text{sch}, \text{ch}} \) \hspace{1cm} \text{Scheduled discharging offer of ESS (MW).}
\( E^D \) \hspace{1cm} \text{Energy of ESS in the DA market (MWh).}
\( E^\text{sch} \) \hspace{1cm} \text{Scheduled energy of ESS (MWh).}
\( P^{\text{ch}, \text{ch}} \) \hspace{1cm} \text{Offer of VPP in the DA market (MW).}
\( P^{\text{ch}, \text{ch}} \) \hspace{1cm} \text{Offer of VPP in the intraday market (MW).}

\( \sigma \) \hspace{1cm} \text{The coefficient of relationship between energy price and load.}
\( D_0 \) \hspace{1cm} \text{The normal value of aggregated loads (MW).}
\( \eta_0 \) \hspace{1cm} \text{Upper limit of curtable load as a fraction of initial load in demand response.}
\( \mu \) \hspace{1cm} \text{The portion of total interruptible load energy with respect to total initial load energy.}
\( S \) \hspace{1cm} \text{The slope of linearized segments.}
\( P_{\text{max}} \) \hspace{1cm} \text{Maximum charging or discharging power of ESS (MW).}
\( E_0 \) \hspace{1cm} \text{Initial energy of ESS (MWh).}
\( d_t \) \hspace{1cm} \text{Duration of time periods (h).}
\( \eta_{\text{ch}}, \eta_{\text{dch}} \) \hspace{1cm} \text{Charging and discharging efficiency of ESS.}
\( E_{\text{min}} \) \hspace{1cm} \text{Minimum energy level of ESS (MWh).}
\( E_{\text{max}} \) \hspace{1cm} \text{Rated energy of ESS (MWh).}

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\[ \delta^{\text{VPP}} \] Positive power deviation of VPP from its scheduled value (MW).
\[ \delta^{-\text{VPP}} \] Negative power deviation of VPP from its scheduled value (MW).
\[ L_{\text{sch},VPP} \] Scheduled curtailable load of VPP (MW).
\[ L_{\text{sch},1,VPP} \] Linearized segments of \( L_{\text{sch},VPP} \) for VPP (MW).
\[ P_{\text{sch},VPP} \] Scheduled offer of VPP (MW).
\[ P_{\text{dch},VPP} \] Charging offer of VPP in the DA market (MW).
\[ P_{\text{dch},1,VPP} \] Discharging offer of VPP in the DA market (MW).
\[ P_{\text{dch,sch},VPP} \] Scheduled charging offer of VPP (MW).
\[ P_{\text{dch,sch},VPP} \] Scheduled discharging offer of VPP (MW).
\[ L_{\text{VPP}} \] Curtailable load offer of VPP in intraday market (MW).
\[ L_{\text{sch},VPP} \] Curtailable load offer of VPP in DA market (MW).
\[ E_{\text{O, VPP}} \] ESS energy of VPP in the DA market (MWh).
\[ E_{\text{ch,sch VPP}} \] Scheduled EES energy of VPP (MWh).

I. INTRODUCTION

A. Motivation and Aim

RENEWABLE energy sources such as wind power can be a viable solution to remedy pollutions and greenhouse gases produced by central large power plants. However, uncertainty of wind generation restricts participation of Wind Power Producers (WPPs) in electricity markets due to energy imbalance costs [1].

Although, there are some supportive solutions for WPPs such as assigning subsidies or special tariffs in order to keep them in markets, these solutions are less compatible with competitive electricity market principles and therefore, a market-based solution is more preferred to increase the penetration level of renewables [2]. Intraday markets have been introduced to give a chance for WPPs to adjust their bids/offers after gate closure of the Day-ahead (DA) market in order to reduce their imbalance costs. Corrections after DA gate closure not only can be beneficial to increase WPP penetration in electricity markets but also can reduce the energy volume and price of real-time balancing markets [3].

In order to cope with the uncertainty of wind energy and therefore to increase the profit and penetration level of WPPs in electricity markets, Demand Response (DR) and Energy Storage System (ESS) are also used in the literature. From WPP uncertainty point of view, DR provides a flexible load profile to be more consistent with uncertain wind power and finally to reduce WPP uncertainty costs. ESSs can also be used to mitigate energy imbalances in the real-time markets [4]. Accordingly, to cope with the wind power uncertainty, Virtual Power Plants (VPPs) can play an active role in electricity markets. Although, DR, ESS, and VPP are employed in the literature for wind energy applications, there is a research gap to model a VPP that jointly employs DR and ESS to increase the profit of WPP in the DA and intraday markets. This model of VPP makes a higher profit for WPP than existing models and consequently, it better prepares the ground for participation of renewable energy sources in the competitive electricity markets.

B. Literature Review

Valuable research is available in literature to incorporate WPPs in different electricity markets. For instance, in [5], a bilevel stochastic model is proposed for strategic offering of a WPP with market power in the DA market as a price maker and in the balancing market as a deviator. Authors in [2] proposed a multi-stage risk-constrained model to derive optimal offering strategy of a WPP to participate in DA and balancing markets as a price maker entity. The application of DR and ESS is also addressed in literature.

Authors in [3] suggested a stochastic framework for WPP participation in different electricity markets (DA and balancing markets) considering DR as uncoordinated operation problem. In [6], a strategic bidding is proposed for a WPP using an energy storage facility to participate in DA and real-time markets with modeling the WPP as a price-taker in the markets. In addition, a VPP, which is composed of WPP and DR, is proposed to mitigate wind uncertainty. Authors in [7] formulated the coordinated operation of WPP and a storage unit in DA and hour-ahead markets. Optimal energy and reserve bids are derived and the stochastic problem is converted to a convex optimization to assure the profitability of private investments on storage units. In [8], the optimal bidding, scheduling, and deployment of battery ESS are studied in the California DA energy market by decomposing the stochastic problem into inner and outer subproblems. Authors in [9] studied DR trading in DA markets using a two-step sequential market clearing.

Similarly, the WPP in the DA market model has been proposed by [10]. In [11], a mechanism of intraday market with considering real-time information of WPPs and shiftable loads has been presented. In this reference, the WPPs make decisions to multiple market transactions in different hours based on the market price. Also, the authors of [12] have formulated the model of the energy bidding problem for VPP with its participants in the regular electricity market and the intraday demand response exchange market. Moreover, the coupon-based DR program is used in [13] to coordinate with WPP to obtain optimal operation in the electricity market. In [14] and [15], the DA market model based on DR capability for congestion management with WPP uncertainty has been proposed. Finally, the capability of flexible resources such as DR and ESS to reduce the curtailed wind energy and virtual bidding as well as increasing system flexibility have been presented in [16] - [18].

C. Contributions

Considering the reviewed literature, the contribution of the current paper is to propose an offering strategy to maximize the profit of a VPP consisting of a WPP, DR, and ESS, entitled wind-demand response-storage, in a coordinated operation in the DA, intraday, and balancing markets. Although these parts of the VPP are separately addressed in the literature, they are not modeled in a coordinated operation by an integrated model of the VPP.

In order to model the uncertainties of wind power and market prices (in DA, intraday, and balancing markets), a scenario-based stochastic programming is used.
The optimization problem is linearized to enhance its computational efficiency and it is formulated as a Mixed-Integer Linear Programming (MILP) problem. The Kantorovich method with a fast forward algorithm is employed for scenario generation and reduction. Different case studies with/without DR and ESS are thoroughly studied and compared; it is inferred that the coordinated operation results in a higher profit of the VPP in the three electricity markets compared with existing literature works. To summarize the unique features of the proposed framework with respect to the previous works in the area, the taxonomy of recent works can be seen in Table I.

Noted that the ES system has been considered in our proposed model. Accordingly, the ES system is capable of storing wind energy during the periods when wind price is low to be used during the periods when wind price is high, thus, WPP can be scheduled with the ES system. A proficient way to dispatch the WPP in electricity markets and manage the WPP volatility is to exploit utility-scale energy storage systems. Also, DRs similar to ES system can play an important role in addressing the issue of wind power scheduling.

D. Paper Organization

The remaining parts of this paper are organized as follows: In Section II, the problem formulation is described in states with/without DR and ESS and the stochastic method used in the paper is briefly explained. Section III includes numerical results and discussions, and Section IV concludes the paper.

II. PROBLEM FORMULATION

In this section, the uncoordinated model of WPP, DR, and ESS is separately represented and afterward, the proposed coordinated model of VPP is presented. In the numerical result section, we follow these models to compare and see the effect of coordinated operation of VPP on its cost.

### TABLE I. TAXONOMY OF RECENT WORKS

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A. The Uncoordinated Model of WPP

The proposed basic model for WPP is formulated [3] as:

$$\max_{P_{d}, P_{i}, \delta_{t}} \sum_{t=1}^{T} \sum_{w=1}^{W_{t}} \mathcal{P}_{d, t \omega} \left[ \lambda_{d, t \omega}^D \delta_{d, t \omega} + \lambda_{i, t \omega}^I \delta_{i, t \omega} + \lambda_{r, t \omega} \delta_{r, t \omega} \right]$$

subject to:

1. Constraints for power deviations:
   \[0 \leq \delta_{d, t \omega} \leq \delta_{d, t \omega}^\text{max} \quad \forall t, \omega (2)\]
   \[0 \leq \delta_{i, t \omega} \leq \delta_{i, t \omega}^\text{max} \quad \forall t, \omega (3)\]
   \[0 \leq \delta_{r, t \omega} \leq \delta_{r, t \omega}^\text{max} \quad \forall t, \omega (4)\]

2. Constraints for energy deviations:
   \[\delta_{d, t \omega} = \delta_{d, t \omega}^\text{max} \quad \forall t, \omega (5)\]
   \[\delta_{i, t \omega} = \delta_{i, t \omega}^\text{max} \quad \forall t, \omega (6)\]
   \[\delta_{r, t \omega} = \delta_{r, t \omega}^\text{max} \quad \forall t, \omega (7)\]

3. Constraints for power balance:
   \[\delta_{d, t \omega} = \delta_{d, t \omega}^\text{max} \quad \forall t, \omega (8)\]
   \[P_{d, t \omega}^D - P_{d, t \omega}^D \left( \lambda_{d, t \omega}^D - \lambda_{d, t \omega}^D \right) \geq 0 \quad \forall t, \omega, \omega', \omega'' (9)\]
   \[P_{d, t \omega}^D = P_{d, t \omega}^D \quad \forall t, \omega, \omega', \omega'' (10)\]
   \[P_{d, t \omega}^D = P_{d, t \omega}^D \quad \forall t, \omega, \omega', \omega'' (11)\]
   \[-\gamma_{d, t \omega} \leq P_{d, t \omega}^D \leq \gamma_{d, t \omega} \quad \forall t, \omega (12)\]

The objective function in (1) maximizes WPP profit. The first and second summation terms represent WPP profits in DA and intraday markets, respectively, whereas the 3rd and 4th terms are WPP profit and cost, respectively, in the balancing market. In (1), we have \(R \geq 1\) and \(R \leq 1\) implying that the generation deficiency of WPP has a higher penalty and its surplus generation is bought with a less price.

Constraint (2) confines the offer of WPP in the DA market to its rated power. The WPP scheduled power in (3) is comprised of its offers in the DA and intraday markets and is limited to WPP rated power by (4). The power deviation of WPP with respect to its scheduled power is given by (5). The positive and negative power deviation results in a profit and cost for WPP, respectively, in the objective function (1). In order to extract the positive and negative deviations, (6)-(8) are imposed. Note that only one of \(\delta^+\) and \(\delta^-\) can be nonzero in one individual time period: \(\delta^+ (\delta^-) = 0 \text{ if } \delta^- (\delta^+) \neq 0\). It is noted that the maximum value of \(\delta^+\) occurs when \(P_{\text{rch}}\) is equal to zero; thus, the upper limit of \(\delta^+\) is set to \(W^\text{max}\) in (7). Also, the maximum of \(\delta^-\) occurs when \(P_{\text{rch}}\) is equal to \(W^\text{max}\); therefore, its upper limit is set to \(W^\text{max}\) in (8). The fact that the offer curve of WPP is not scenario dependent is constrained by (9)-(11). The intraday market is in fact developed to modify the DA offer by a given value. The portion of intraday offer with respect to the DA market is expressed by (12), where the coefficient \(\gamma\) is decided by the market operator.

B. The Uncoordinated Model of Aggregated DR

The proposed model for DR is formulated as [3]:

$$\max_{L_{d, t \omega}^D, L_{i, t \omega}^D} \sum_{t=1}^{T} \sum_{w=1}^{W_{t}} \mathcal{P}_{d, t \omega} \left[ \lambda_{d, t \omega}^D L_{d, t \omega}^D + \lambda_{i, t \omega}^I L_{i, t \omega}^D + \lambda_{r, t \omega} L_{r, t \omega} + \lambda_{r, t \omega}^I L_{r, t \omega} \right] + \frac{1}{2} \sigma_{D_{t \omega}}^2$$

The first and second summation terms represent WPP profits in DA and intraday markets, respectively, whereas the 3rd and 4th terms are WPP profit and cost, respectively, in the balancing market. In (1), we have \(R \geq 1\) and \(R \leq 1\) implying that the generation deficiency of WPP has a higher penalty and its surplus generation is bought with a less price.

Constraint (2) confines the offer of WPP in the DA market to its rated power. The WPP scheduled power in (3) is comprised of its offers in the DA and intraday markets and is limited to WPP rated power by (4). The power deviation of WPP with respect to its scheduled power is given by (5). The positive and negative power deviation results in a profit and cost for WPP, respectively, in the objective function (1). In order to extract the positive and negative deviations, (6)-(8) are imposed. Note that only one of \(\delta^+\) and \(\delta^-\) can be nonzero in one individual time period: \(\delta^+ (\delta^-) = 0 \text{ if } \delta^- (\delta^+) \neq 0\). It is noted that the maximum value of \(\delta^+\) occurs when \(P_{\text{rch}}\) is equal to zero; thus, the upper limit of \(\delta^+\) is set to \(W^\text{max}\) in (7). Also, the maximum of \(\delta^-\) occurs when \(P_{\text{rch}}\) is equal to \(W^\text{max}\); therefore, its upper limit is set to \(W^\text{max}\) in (8). The fact that the offer curve of WPP is not scenario dependent is constrained by (9)-(11). The intraday market is in fact developed to modify the DA offer by a given value. The portion of intraday offer with respect to the DA market is expressed by (12), where the coefficient \(\gamma\) is decided by the market operator.
subject to:
\[
L_{ch,\omega}^\omega = L_{c,\omega}^D + I_{c,\omega}^D \quad \forall t, \forall \omega
\]  \hspace{1cm} (14)
\[
0 \leq L_{c,\omega}^D \leq \eta D_{c,\omega} \quad \forall t, \forall \omega
\]  \hspace{1cm} (15)
\[
0 \leq L_{ch,\omega}^\omega \leq D_{ch,\omega} \quad \forall t, \forall \omega
\]  \hspace{1cm} (16)
\[
\sum_{j=1}^{N_j} L_{ch,\omega}^\omega \leq \mu \sum_{j=1}^{N_j} D_{ch,\omega} \quad \forall \omega.
\]  \hspace{1cm} (17)

The objective function in (13) maximizes DR profit: the first two summation terms are the money paid to demands with the normal energy price rates in DA and intraday markets. In addition, demands are paid an incentive payment with a fixed rate as modeled by the third and fourth summation terms. The last term of the summation expresses DR profit considering elastic demand by using the exponential benefit function [3]. The scheduled curtailable load energy (in DA and intraday markets) to its fraction of initial load. Constraint (17) limits the scheduled curtailable DR power is expressed as:

\[
\text{Max} \quad \sum_{\omega=1}^{\omega=\omega} \left[ \lambda_{c,\omega}^D L_{c,\omega}^D + \lambda_{ch,\omega}^D L_{ch,\omega}^\omega + \lambda_{D,\omega}^D \right] + \sum_{\omega=1}^{\omega=\omega} \left[ \lambda_{c,\omega}^I I_{c,\omega}^I + \lambda_{ch,\omega}^I I_{ch,\omega}^\omega + \lambda_{D,\omega}^I \right]
\]  \hspace{1cm} (18)

subject to:
\[
L_{ch,\omega}^\omega = \sum_{j=1}^{N_j} t_{ch,\omega}^j \quad \forall t, \forall \omega
\]  \hspace{1cm} (19)

Constraints (14)-(17).

C. The Uncoordinated Model of ESS

The proposed model for ESS is formulated as:

\[
\text{Max} \quad P_{ch,\omega}^D, P_{c,\omega}^D, P_{ch,\omega}^I, P_{c,\omega}^I, N_{ch,\omega} \sum_{\omega=1}^{\omega=\omega} \left[ \lambda_{c,\omega}^D \left( P_{ch,\omega}^D - P_{c,\omega}^D \right) + \lambda_{c,\omega}^I \left( P_{ch,\omega}^I - P_{c,\omega}^I \right) \right]
\]  \hspace{1cm} (20)

subject to:
\[
P_{ch,\omega}^D = P_{c,\omega}^D \quad \forall t, \forall \omega
\]  \hspace{1cm} (21)
\[
P_{c,\omega}^D = P_{c,\omega}^D + P_{ch,\omega}^I \quad \forall t, \forall \omega
\]  \hspace{1cm} (22)
\[
0 \leq P_{ch,\omega}^D \leq P_{\max} y_{\omega} \quad \forall t, \forall \omega
\]  \hspace{1cm} (23)
\[
0 \leq P_{c,\omega}^D \leq P_{\max} \left(1 - y_{\omega} \right) \quad \forall t, \forall \omega
\]  \hspace{1cm} (24)
\[
0 \leq P_{ch,\omega}^I \leq P_{\max} y_{\omega} \quad \forall t, \forall \omega
\]  \hspace{1cm} (25)
\[
0 \leq P_{c,\omega}^I \leq P_{\max} \left(1 - y_{\omega} \right) \quad \forall t, \forall \omega
\]  \hspace{1cm} (26)
\[
E_{c,\omega}^D = E_{c,\omega}^D + du \left( \eta_{D,\omega} P_{ch,\omega}^D - \frac{1}{\eta_{ch}} P_{c,\omega}^D \right) \quad \forall t = 1, \forall \omega
\]  \hspace{1cm} (27)

The profit of ESS is maximized by the objective function of (20), where the first and second summation terms refer to ESS profit in the DA and intraday markets, respectively. The scheduled charging power of ESS is sum of its offers in DA and intraday markets as expressed by (21). Similarly, the discharging power is given by (22). The charging and discharging offer of ESS in the DA market is constrained by (23) and (24), respectively, where \( y_{\omega} \) as a binary variable determines whether the ESS is being charged. Similarly, (25) and (26) constrain the scheduled charging and discharging offers of ESS, respectively. The stored energy of ESS in the DA market is formulated by (27) and (28) for the first and other time periods, respectively. In these equations, the charging and discharging efficiency of ESS is taken into account. Equations (29) and (30) similarly give the scheduled energy of ESS. Finally, (31) and (32) confine ESS energy to its lower and upper limits.

D. The Proposed Model for VPP

In the previous subsections, uncoordinated models of WPP, DR, and ESS are reviewed. As it can be seen in Fig. 1, in the uncoordinated operation, WPPs and ESSs submit their generation scheduling offer and the DRPs submit their reduction bid, independently. According to the proposed model in Fig. 1, for the coordinated scheme, for the joint operation of WPP, DR, and ESS, a central decision maker is required. The so called VPP is directly responsible for participating in all three markets (day-ahead, intraday, and balancing markets). Accordingly, firstly, VPP gathers the information of WPP (e.g., predicted wind power), ESS (status of charge, charging and discharging efficiencies) and DRP (e.g., load shifting/reduction capability, initial hourly load) and afterwards, decides the best offering strategy by forecasting market prices based on the latest information, technical constraints and market rules. Here, we formulate a VPP model consisting of a WPP, DR, and ESS. Using the coordinated operation of these resources, the profit of VPP in different markets are higher than uncoordinated operations. The complete form of the proposed VPP model is as follows:

\[
\text{Max} \quad P_{ch,\omega}^{VPP}, P_{c,\omega}^{VPP}, \delta_{ch,\omega}^{VPP}, \delta_{c,\omega}^{VPP} \sum_{\omega=1}^{\omega=\omega} \sum_{t=1}^{t=\omega} \left[ \lambda_{c,\omega}^{VPP} \left( P_{ch,\omega}^{VPP} - P_{c,\omega}^{VPP} \right) + \lambda_{ch,\omega}^{VPP} \left( P_{ch,\omega}^{VPP} - P_{c,\omega}^{VPP} \right) \right]
\]  \hspace{1cm} (33)
subject to:

\[
0 \leq P_{t,\omega}^{D,VPP} \leq W_{\max} + \eta_t D_{\omega,t} + P_{\max} (1 - y_t) - P_{\max} y_t \quad \forall t, \forall \omega \tag{34}
\]

\[
P_{t,\omega}^{W,VPP} = P_{t,\omega}^{D,VPP} + L_{t,\omega,1}^{Y,VPP} \quad \forall t, \forall \omega \tag{35}
\]

\[
0 \leq P_{t,\omega}^{D,Y,VPP} \leq W_{\max} + \eta_t D_{\omega,t} + P_{\max} (1 - y_t) - P_{\max} y_t \quad \forall t, \forall \omega \tag{36}
\]

\[
0 \leq P_{t,\omega}^{D,Y,VPP} \leq L_{t,\omega,1}^{Y,Y,VPP} \quad \forall t, \forall \omega \tag{37}
\]

\[
0 \leq \delta_{t,\omega}^{D,Y,VPP} \leq W_{t,\omega}^{Y,Y,VPP} \quad \forall t, \forall \omega \tag{38}
\]

\[
0 \leq \delta_{t,\omega}^{D,VPP} \leq W_{t,\omega}^{VPP} + L_{t,\omega,1}^{VPP} \quad \forall t, \forall \omega \tag{39}
\]

\[
( P_{t,\omega}^{D,VPP} - P_{t,\omega}^{D,Y,VPP} ) ( \lambda_{t,\omega}^{D} - \lambda_{t,\omega}^{D,Y} ) \geq 0 \quad \forall t, \forall \omega, \forall \omega' \tag{41}
\]

\[
P_{t,\omega}^{D,VPP} = P_{t,\omega}^{D,Y,VPP} \quad \forall t, \forall \omega, \forall \omega', \lambda_{t,\omega}^{D} = \lambda_{t,\omega}^{D,Y} \tag{42}
\]

\[
P_{t,\omega}^{D,Y,VPP} = P_{t,\omega}^{D,Y,Y,VPP} \quad \forall t, \forall \omega, \forall \omega', \lambda_{t,\omega}^{D,Y} = \lambda_{t,\omega}^{D,Y,Y} \tag{43}
\]

\[
L_{t,\omega}^{Y,Y,VPP} = L_{t,\omega}^{Y,VPP} + L_{t,\omega}^{Y,VPP} \quad \forall t, \forall \omega \tag{44}
\]

\[
L_{t,\omega}^{Y,Y,Y,VPP} = L_{t,\omega}^{Y,VPP} - L_{t,\omega}^{Y,VPP} \quad \forall t, \forall \omega \tag{45}
\]

\[
0 \leq L_{t,\omega}^{Y,VPP} \leq \eta_t D_{\omega,t} \quad \forall t, \forall \omega \tag{46}
\]

\[
0 \leq L_{t,\omega}^{Y,Y,VPP} \leq \eta_t D_{\omega,t} \quad \forall t, \forall \omega \tag{47}
\]

\[
0 \leq \delta_{t,\omega}^{Y,Y,VPP} \leq \delta_{t,\omega}^{Y,VPP} \quad \forall t, \forall \omega \tag{48}
\]

\[
L_{t,\omega}^{Y,VPP} = \sum_{i=1}^{N_t} L_{t,\omega}^{Y,VPP} \quad \forall t, \forall \omega \tag{49}
\]

\[
L_{t,\omega}^{Y,Y,VPP} = \sum_{i=1}^{N_t} L_{t,\omega}^{Y,Y,VPP} \quad \forall t, \forall \omega \tag{50}
\]

\[
P_{t,\omega}^{D,Y,VPP} = P_{t,\omega}^{D,Y,Y,VPP} \quad \forall t, \forall \omega, \forall \omega', \lambda_{t,\omega}^{D,Y} = \lambda_{t,\omega}^{D,Y,Y} \tag{51}
\]

\[
E_{t,\omega}^{D,Y,VPP} = E_{t,\omega}^{D,Y,VPP} + du \left( \eta_t P_{t,\omega}^{D,Y,VPP} - \frac{1}{\eta_{t,\omega}} P_{t,\omega}^{D,Y,VPP} \right) \quad \forall t, 1, \forall \omega \tag{52}
\]

\[
E_{t,\omega}^{D,Y,Y,VPP} = E_{t,\omega}^{D,Y,Y,VPP} + du \left( \eta_t P_{t,\omega}^{D,Y,Y,VPP} \frac{1}{\eta_{t,\omega}} \right) \quad \forall t, 1, \forall \omega \tag{53}
\]

\[
E_{t,\omega}^{D,Y,VPP} = E_{t,\omega}^{D,Y,VPP} + du \left( \frac{1}{\eta_{t,\omega}} P_{t,\omega}^{D,Y,VPP} \right) \quad \forall t, 1, \forall \omega \tag{54}
\]

\[
E_{t,\omega}^{D,Y,VPP} = E_{t,\omega}^{D,Y,VPP} + du \left( \frac{1}{\eta_{t,\omega}} P_{t,\omega}^{D,Y,VPP} \right) \quad \forall t, 1, \forall \omega \tag{55}
\]

\[
E_{t,\omega}^{D,Y,VPP} = E_{t,\omega}^{D,Y,VPP} + du \left( \frac{1}{\eta_{t,\omega}} P_{t,\omega}^{D,Y,VPP} \right) \quad \forall t, 1, \forall \omega \tag{56}
\]

\[
E_{t,\omega}^{D,Y,VPP} = E_{t,\omega}^{D,Y,VPP} + du \left( \frac{1}{\eta_{t,\omega}} P_{t,\omega}^{D,Y,VPP} \right) \quad \forall t, 1, \forall \omega \tag{57}
\]

\[
E_{t,\omega}^{D,Y,VPP} = E_{t,\omega}^{D,Y,VPP} + du \left( \frac{1}{\eta_{t,\omega}} P_{t,\omega}^{D,Y,VPP} \right) \quad \forall t, 1, \forall \omega \tag{58}
\]

\[
E_{t,\omega}^{D,Y,VPP} = E_{t,\omega}^{D,Y,VPP} + du \left( \frac{1}{\eta_{t,\omega}} P_{t,\omega}^{D,Y,VPP} \right) \quad \forall t, 1, \forall \omega \tag{59}
\]

\[
E_{t,\omega}^{D,Y,VPP} = E_{t,\omega}^{D,Y,VPP} + du \left( \frac{1}{\eta_{t,\omega}} P_{t,\omega}^{D,Y,VPP} \right) \quad \forall t, 1, \forall \omega \tag{60}
\]

\[
E_{t,\omega}^{D,Y,VPP} = E_{t,\omega}^{D,Y,VPP} + du \left( \frac{1}{\eta_{t,\omega}} P_{t,\omega}^{D,Y,VPP} \right) \quad \forall t, 1, \forall \omega \tag{61}
\]
Note, this variable shows the load shifting/reduction in VPP. Finally, the constraints (52)-(61) formulate the ESS part of the VPP using variables \( P_{\omega_1,t}^{h,h,VPP} \) and \( P_{\omega_2,t}^{h,s,VPP} \).

E. Stochastic Programming Method

WPPs face two major sources of uncertainty: availability of the wind generation and market prices (DA, ID, and Balancing). In addition, DRP and ESS problem described above is subject to the uncertainty of DA and ID market prices. In order to deal with these uncertainties, the coordinated offering strategy of VPP has been modeled as stochastic processes. To this end, a multi-stage stochastic programming is employed to solve offering strategy of VPP. Each stage refers to each market (DA, ID and Balancing) including first-stage (here-and-now), second-stage (wait-and-see1) and third-stage (wait-and-see2). Decision making of the first stage should be specified before the realization of the scenarios. Accordingly, the first-stage decision variables are related to the DA market variables. When the DA market prices are known for each time horizon, the decision variables of the second stage should be determined for each possible realization of DA market prices. Finally, decision variables of the third stage of the stochastic programming refers to the balancing market. In this paper, we follow a stochastic programming method based on [20-22].

In the proposed method, we assume that WPP generation as well as prices of the DA, intraday, and balancing markets are uncertain parameters. These parameters are forecasted in advance and we formulate their forecast errors using appropriate Probability Distribution Functions (PDFs) [20]. Then, the roulette wheel mechanism [21] is used to generate possible joint scenarios. In order to enhance the computational efficiency of the stochastic programming, the Kantorovich method [22] is applied for scenario reduction. The number of scenarios that are generated for the above-mentioned stochastic parameters in the proposed method are as:

- \( N_W \) scenarios for the wind power generation.
- \( N_D \) scenarios for DA market price (\( \lambda^D \)).
- \( N_I \) scenarios for intraday market price (\( \lambda^I \)).
- \( N_B \) scenarios for balancing market price (\( R^+ \), \( R^- \)).

As a result, the total number of combinational scenarios in the proposed method will be \( N_W \cdot N_D \cdot N_I \cdot N_B \). In the case study, we assumed 10, 10, 5, 6 for \( N_W, N_D, N_I \) and \( N_B \), respectively, resulting in total number of 3000 combinational scenarios. Finally, noted that further details about the proposed scenario generation/reduction algorithm can be found in [23].

III. NUMERICAL RESULTS

The proposed method is here tested on the Spanish Sotavento wind farm [24] with the rated capacity of 17.56 MW. This WPP is considered with an ESS with the specifications listed in Table II [25]. The system load data and energy prices for DA and intraday markets are adopted from the Iberian Peninsula market [26]. Our study is carried out on a week spanning 7-13 March 2010 of this market.

In the following subsections of A-D, we focus on the first day of the week (March 7 of 2010) to better focus on the results. However, in subsection E, we present results for the whole week. Parameters of the proposed method as used in the simulations are 0.3, 0.04, -0.3, 0.2, and 0.3 $/MWh for \( \gamma, \mu, \sigma, \eta_i, \) and \( \lambda_i \), respectively [23]. The DA market price is a random parameter in the proposed method; its mean values are depicted in Fig. 2 for days of the week under study [26].

In Fig. 3, the initial hourly load before curtailing is presented for days of the week [26]. In order to solve optimization problems, we used here the GAMS software and CPLEX solver [27]. In the subsequent parts, results are presented in different uncoordinated and coordinated modes in order to compare them and evaluate the performance of the proposed joint operation of VPP. Results presented in following subsections are resulted from stochastic programming as a weighted sum of parameters using probability of scenarios. It is noted that, the day-ahead scheduling power for WPP, ESS and DR are defined by variables \( P_{\omega_1,t}^{D,VPP}, P_{\omega_2,t}^{D,VPP} \) and \( \{ P_{\omega_1,t}^{D,D,VPP}, P_{\omega_2,t}^{D,D,VPP} \} \), with superscript \( D \), respectively. The hourly power scheduling of WPP, ESS, DR and VPP is obtained using objective function (33), equations (45) and (52)-(53).

A. Optimal Uncoordinated Operation of WPP

The problem in this section is formulated by (1)-(12) as a Linear Programming (LP) model. The optimal hourly bid of WPP in the DA and intraday markets as obtained after solving the model is plotted in Fig. 4. As seen, the WPP participated with its full capacity (17.56 MW) when the price is higher (see Fig. 2) in order to maximize its profit in DA, intraday, and balancing markets. The hourly expected profit of WPP is also depicted in Fig. 5. As seen, WPP obtain its profit majorly from the DA market. Total profit of WPP from the three markets is equal to $4721.
TABLE II. ENERGY STORAGE SYSTEM SPECIFICATIONS

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Initial energy (MWh)</td>
<td>5</td>
</tr>
<tr>
<td>Minimum energy (MWh)</td>
<td>2</td>
</tr>
<tr>
<td>Maximum energy (MWh)</td>
<td>25</td>
</tr>
<tr>
<td>Maximum charging/discharging power (MW)</td>
<td>4</td>
</tr>
</tbody>
</table>

B. Optimal Uncoordinated Operation of Aggregated DR

The problem in this case is formulated by (14)-(19) as an LP model. The optimal curtailable DR offer and its profit is depicted in Fig. 6 and Fig. 7, respectively, for March 7 of 2010. As seen, DR is more sensitive than WPP to price signals and its offer happens only in peak hours of the market. That is, only when the energy price is high, it is profitable for DR to participate in the market.

As seen in Fig. 3 (the March 7, 2010 curve), the load demand at peak hours is about 17 MW before DR. The participation of DR reduces this peak demand by about 3 MW at peak hours as seen in Fig. 6. Total profit of DR from the three markets of DA, intraday, and balancing is equal to $1200.

C. Optimal Uncoordinated Operation of ESS

The optimization problem in this case is modeled by (20)-(32) as an MILP. The optimal offer of ESS in the DA market is plotted in Fig. 8 and the expected profit of ESS is shown in Fig. 9.

As seen in Fig. 8, the ESS is charged in off-peak and mid-peak hours and it is discharged in on-peak hours. That is, the energy is bought in low-tariff hours and it is sold in high-tariff hours in order to maximize ESS profit.

Although the ESS optimization problem of (20)-(32) includes its offers in both DA and intraday markets, it is not profitable for ESS to participate in the intraday market and then, it participates only in the DA market as seen in Fig. 8. Total profit of ESS is equal to $662.

D. Optimal Coordinated Operation of VPP

The VPP in this case includes the joint optimization of WPP, DR, and ESS as formulated by (33)-(61) as an MILP model. The VPP optimal offer and its expected profit are plotted in Fig. 10 and Fig. 11, respectively.
As seen in Fig. 10, the VPP offer has increased to about 25 MW at peak hours compared with the uncoordinated operation of WPP with 17.56 MW offer. In fact, VPP employs DR and ESS in addition to WPP as generation assets to more increase its profit at peak hours with higher tariffs. Total expected profit of VPP over the 24 hours has been $7810. In the subsection, we compare the profit of VPP with individual uncoordinated operations of WPP, DR, and ESS.

E. Comparison

Results of uncoordinated operations of WPP, DR, and ESS as well as the coordinated operation of VPP are presented in previous subsections for the first day (7 March, 2010) of the week under study. In Table III, the summary of expected profits of uncoordinated and coordinated cases are presented for all days of the week under study. Also, sum of profits of the three uncoordinated operations is shown in the table. In addition, the coordinated operation of VPP (including WPP, DR, and ESS) is reported in the second part of Table III. Under column “%” of this table, profits of $4721 (for WPP), $1200 (for DR), $662 (for ESS), and $7810 (for VPP) are previously reported in preceding subsections. Considering the first day of the week (March 7 of 2010) in this table, sum of uncoordinated profits of WPP, DR, and ESS is equal to $6583 (4721 + 1200 + 662), whereas their coordinated operations in the VPP results in the profit of $7810, which is considerably higher than uncoordinated operations (18.64%). The gain in profit due to the coordinated VPP with respect to sum of uncoordinated operations is reported in the last row of the table for all days of the week. A higher profit implies a higher incentive for VPP to be participated in electricity markets using our proposed model. In other words, the proposed model increases the ability of WPPs in electricity markets without any need to supportive or subsidizing mechanisms.

This trend finally rises the penetration level of renewable energies in electricity markets. Not only the WPP power increases under the VPP framework, but also DR and ESS participate more effectively. For instance, the participation of DR in the DA market for the two cases is plotted in Fig. 112 for 7 March 2010. As seen, in the uncoordinated operation, the DR participates in limited hours with only positive values implying only load curtailment. However, in case of VPP coordinated operation, DR participates in extended hours with both positive and negative offers. The ultimate result is that the expected profit of the VPP increases in case of coordinated operation. In addition to increasing the profit of VPP, total energy supplied by WPP, DR and ESS in the three markets also increase. In Table IV, the energy supplied by coordinated and uncoordinated cases is mentioned for the considered week.

For instance, in the first day, total energy supplied by uncoordinated operations of WPP, DR, and ESS is 6583 MWh, whereas it is 7810 MWh in case of coordinated operation of VPP. Considering the whole week, total supplied energy over the week is 70.471 GWh and 78.313 GWh for uncoordinated and coordinated operations, respectively. This means that penetration level of renewable energies (WPP+ESS+DR) increases by 11.1% by the coordinated operation. As a result, the proposed coordinated operation increases not only the participation of renewables but also their profits, Table V. It is noted that these gains are obtained by a market-based framework, not by a subsidizing mechanism to support renewables. In other words, the main advantage of the proposed VPP framework is to promote renewable energy in electricity markets without any need to subside mechanisms, a development which is more consistent with electricity markets principles.

F. Sensitivity Analysis for Degree of Coordination

Here, the sensitivity analysis is done to determine the degree of coordination of the VPP’s expected profit with respect to the variations of the capacity for WPP, DR and ESS as well as DA and ID market prices’ change.
Accordingly, the results have been shown in Table V. As it is seen in this table, the increment value (%) of each parameter has been changed from 0% to 30%. Results show increasing trend in the value of expected profit for the VPP by increasing different parameters. In the last row of Table V, the sensitivity factor of the expected profit of VPP with respect to the variations of each parameter has been addressed. For variations of the size for WPP, DR and ESS, the sensitivity factor has the approximate constant value. However, changing the DA and ID market prices reveals nonlinear change of the degree of coordination, because by changing the price, the degree of coordination of the WPP, DR and ESS will be changed for each hour.

<table>
<thead>
<tr>
<th>Increment (ζ %)</th>
<th>0</th>
<th>10</th>
<th>20</th>
<th>30</th>
<th>Deviation</th>
</tr>
</thead>
<tbody>
<tr>
<td>VPP profit ($)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>WPP size</td>
<td>7810</td>
<td>8283</td>
<td>8756</td>
<td>9228</td>
<td>+0.605*ζ</td>
</tr>
<tr>
<td>DR size</td>
<td>7810</td>
<td>8051</td>
<td>8293</td>
<td>8534</td>
<td>+0.308*ζ</td>
</tr>
<tr>
<td>ESS size</td>
<td>7810</td>
<td>7877</td>
<td>7944</td>
<td>8010</td>
<td>+0.086*ζ</td>
</tr>
<tr>
<td>DA market price</td>
<td>7810</td>
<td>8531</td>
<td>9372</td>
<td>10153</td>
<td>(0.923 to 1)*ζ</td>
</tr>
<tr>
<td>ID market price</td>
<td>7810</td>
<td>7943</td>
<td>8201</td>
<td>8653</td>
<td>+0.17 to 0.36*ζ</td>
</tr>
</tbody>
</table>

### IV. CONCLUSIONS

This paper presented a framework to maximize the profit of VPP, including a WPP, DR, and ESS in day-ahead, intraday, and balancing electricity markets. First, uncoordinated operations of WPP, DR, and ESS were formulated. Then, a model was proposed for the coordinated operation of VPP to maximize its profit for more efficiently managing power system assets. Scenarios of stochastic programming were generated using a joint scenario tree and the Kantorovich method was used for scenario reduction. The proposed framework was tested on a Spanish wind farm and was compared with previous methods. According to the obtained results, it was determined that the proposed VPP leads to both a higher participation of wind energy and a higher profit; for instance, in the first day of the week under study, it leads to 18.64% more profit and 11.1% more renewable energy participation compared with uncoordinated operations. The proposed method considers the simultaneous participation in three markets, so, a further work is needed to establish the optimization of scheduling in the intraday market. In fact, transactions in the intraday market are always in the form of bilateral contract which means that there could be lots of different prices in the same hour. Hence, investigation and experimentation into optimization in this market is strongly recommended.

### REFERENCES


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