A Single Synchronous Controller for High Penetration of Renewable Energy Resources into the Power Grid

Abstract—A single synchronous controller (SSC) technique is proposed in this paper for control of interfaced converters under high penetration of renewable energy resources (RER) into the power grid. The proposed SSC is based on a new dynamic model concerning to the power grid stability (PGS) and modeled based on all features of a synchronous generator (SG), which can properly improve the performance of the power grid in those scenarios in which a large-scale penetration of RERs is considered. Different transfer functions are achieved to assess the high performance of the proposed control technique. Simulation results are presented to demonstrate the superiority of the proposed SSC in the control of the power electronic-based synchronous generator under high penetration of RERs into the power grid.

Keywords—Single synchronous controller (SSC), Low-value inertia, Virtual mechanical power (VMP), Virtual angular frequency (VAF), Renewable energy resources (RERs).

I. INTRODUCTION

The important roles of distributed generation technology especially based on renewable energy resources (RERs) in power system [1]-[3] and different concerns associated to the instable operation of power grid under high penetration of RERs have been studied highly in the literature in recent years.

In some studies authors focused on using distributed energy storage systems (DESSs) for encountering such stability problems counter them through the design of an optimized supervisory and advanced controllers for large-scale DESSs with the aim of reliable and stable integration of RERs with the power grid [4]-[6].

In other studies in order to compensate the voltage rise of the power grid caused by the excess of PV sources, the reactive power based controllers proposed for the interfaced converters in DG units [7]-[9].

In this paper, a single synchronous controller (SSC) is proposed based on an active and reactive power-based dynamic model with the aim of providing a stable operation for the power grid under high penetration of RERs.

The rest of this paper is organized as follows. Achieving the proposed active and reactive power based dynamic model is presented in the first subsection of Section II. Then, the Section II is completed by designing the proposed SSC. Two transfer functions are obtained in Section III to assess the effects of different parameters related to the SSC on the ability of the SSC at presenting accurate active and reactive power sharing as well as power grid stability (PGS). Finally, simulation results are given in Section IV and conclusions are drawn in Section V.

II. PROPOSED MODEL

The general model based on the interfaced-converter for integration of large-scale RERs is drawn in Fig. 1. This figure contains the power grid, loads, permanent magnet synchronous generator (PMSG), two types of controllable RER, and grid-feeding RERs which will be discussed further in the subsequent sections.

A. The Mathematical Model Description

The dynamic model of the proposed model in Fig. 1 should be extracted in order to draw a control technique for control of the interfaced converter for integration of large-scale RERs into the power grid.

By this assumption, the dynamic equations of the proposed model in dq reference frame can be expressed as [10]:

\[
L_\alpha \frac{dq}{dt} + R_i q - \omega L_i q - u_i i_{\alpha} = v_{\alpha} = 0
\]

(1)

\[
L_\beta \frac{d\varphi}{dt} + R_\varphi \varphi + \omega L_\varphi \varphi - u_\varphi i_{\beta} = v_{\varphi} = 0
\]

(2)

\[
C \frac{dv_{\alpha}}{dt} + u_{\alpha} i_{\alpha} + u_\varphi i_{\varphi} + i_{\beta} = 0
\]

(3)

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(3)

The instantaneous active and reactive power of RER-based interfaced converter (REIC) can be stated as \(P = i_{\alpha} v_{\alpha}\) and \(Q = -i_{\beta} v_{\alpha}\). By neglecting the partial variations, a set of new active and reactive power based dynamic equations can be obtained through multiplying the d-component of the reference voltage \(v_{\alpha}\) to (1)-(3).
Consider the swing equation of a SG as:

\[ \Delta \omega = \frac{1}{\omega J} \left( \frac{P_n - P}{s + \left( P_n - P \right) / \omega^2 J} \right) \Delta \omega \]  

Equations (8) and (9) can lead to constructing an important part of the ultimate controller consisted of all properties of SG as shown in Fig. 2. As it is depicted, the error parts of VMP and VAF are utilized for the active power-axis of the SSC. Moreover, the scenario used for achieving the virtual angular frequency can be employed for both active and reactive-axis of the proposed SSC.

By considering a low pass filter (LPF) as \( \omega_s / (s + \omega_s) \), LPF coefficients and the coefficients of PI controller associated with virtual angular frequency error can be driven as:

\[ \alpha_1 = \frac{1}{\omega_s}, \quad \alpha_2 = \left( P_n - P' \right) / \omega^2 J \]  

\[ k_{pp} = \omega_s J, \quad k_{pp} = \left( P_n - P' \right) / \omega^2 J' \]

It can be understood from (10) and (11) that all coefficients are highly dependent on inertia, reference values of active power, VMP, and VAF.

**B.2. The Proposed Controller**

According to Fig. 2, the active and reactive axis of the proposed control technique can be written as:

\[ u_1 = \frac{1}{P_z} \left( \left( \Delta P - P_n \right) \left( k_{pp} + k_{qq} / s \right) + \left( \Delta \omega \right) \left( k_{pp} + k_{qq} / s \right) \right) \]  

\[ u_q = -\frac{1}{P_z} \left( \left( \Delta P - P_n \right) \left( \frac{\alpha_1}{s + \omega_2} + \omega_s \right) \right) \]  

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where, \( J, \omega, P, \) and \( P_n \) are moment inertia, angular frequency, electrical power, and mechanical power of SG respectively. Using the small-signal linearization for (7) and performing some simplifications, (8) can be achieved as:

\[ \Delta \omega = \frac{1}{\omega J} \left( \frac{P_n - P}{s + \left( P_n - P \right) / \omega^2 J} \right) \Delta \omega \]  

where, \( P_c, q \) are known, the swing equation of a SG can be stated as:

\[ L \frac{dP}{dt} + P + \frac{Q}{R} Q = u_s P_c + P_2 = 0 \]  

\[ L \frac{dQ}{dt} + Q + \frac{Q}{R} P + u_s P_c = 0 \]  

\[ RC \frac{dP_c}{dt} + u_s P_c - u_s Q + P_2 = 0 \]  

where, \( P_c, q \) are \( V_d, V_d / R, P_d = V_d / R, \) and \( P_d = V_d / R. \)

**B.1. The SG Characteristics Extraction**

The major concerns associated with high penetration of RERs are the unstable behaviors of the voltage magnitude and the frequency of the power grid due to odd transient dynamics of interfaced converters and the lack of inertia of this kind of generators [11]. These concerns can be noticeably decreased by considering all the properties of synchronous generators in the structure of the control loop of interfaced converter. As it is known, the swing equation of a SG can be stated as:

\[ j \frac{d\omega}{dt} = \frac{P_n - P}{\omega} \]  

where, \( J, \omega, P, \) and \( P_n \) are moment inertia, angular frequency, electrical power, and mechanical power of SG respectively. Using the small-signal linearization for (7) and performing some simplifications, (8) can be achieved as:

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\[ \frac{\Delta P}{s} = \frac{\Delta P_n}{s} - \left( \omega J + \left( P_n - P \right) / \omega^2 J \right) \Delta \omega \]  

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\[ \frac{1}{P_z} \left( \left( \Delta P - P_n \right) \left( \frac{\alpha_1}{s + \omega_2} + \omega_s \right) \right) \]
Equations (13) and (14) show that both d and q axis of the SSC are affected by the features of the SG. This advantage can significantly cause the added inherent features of the SG to make more contributions in the operation of REIC in power grid stability under high penetration of RERs. This advantage is analyzed in the next sections.

III. ACTIVE AND REACTIVE POWER SHARING EVALUATION

As can be seen from Fig. 2, both active and reactive power and their reference values are used as output and input of closed-loop descriptions of the SSC, respectively. The coefficients of $\alpha$ and $\beta$ are the decoupled factors of closed loop descriptions that can vary the amount of decoupled relationship between the active component of the SSC and the reactive power and vice versa.

In fact, these coefficients make relationship between $P$ and $Q$ in the SSC. By considering two closed-loop diagrams in Fig. 2, two transfer functions related to active and reactive power are driven as:

$$\frac{P}{P^*} = \left(\frac{Lk_p}{R}\right)^* s^3 + \left[\left(\frac{L}{R}\right)\left(k_p + k_{s2}a_1 - a_1k_{s2}\right) + \left(k_p + k_{s1}a_1 - a_1k_{s1}\right)\right]s^2 + \left[\left(\frac{L}{R}\right)\left(k_p - k_{s2}a_1\right) + \left(k_p + k_{s1}a_1 - a_1k_{s1}\right)\right]s + \left(k_pa_1 - a_1k_p\right)\frac{L}{R}$$

$$\frac{Q}{Q^*} = \frac{k_{pp}s + k_{qq}}{(L/R)s^2 + (1+k_{pp})s + k_q}$$

Equation (15) shows that the transfer function related to the active power of REIC and its reference value are highly dependent on the SG features and its related controllers. The Nyquist diagrams of $P/P^*$ for various low-value inertias are drawn in Fig. 3.

As can be seen for the smallest inertia value, the ratio of $P/P^*$ is extremely near to 1 around the reference of the angular frequency that confirms the accurate active power tracking of the proposed SSC in this condition.

Also, the aforementioned explanation is true for $J_2$ with slightly less accuracy. Instead, for $J_3$ and $J_4$, the active power of the SSC is not able to track its reference value as can be seen in Fig. 3.

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**Fig. 3.** The Nyquist diagram of $P/P^*$ for different inertia values $J_4>J_3>J_2>J_1$: (a) $J_1$, (b) $J_2$, (c) $J_3$, (d) $J_4$. 
The phase and bode diagrams of \( P/P^* \) illustrated in Fig. 4, further confirm the aforementioned discussions. Based on this figure, for two first low-value inertias, the phases of this ratio is near to zero around the reference of the angular frequency. However, this is not valid for last two values of \( J_3 \) and \( J_4 \). On the other hand, it is apparently seen from (16) that the reactive power component of the SSC is not concerned with SG characteristics.

Fig. 5 and Fig. 6 show the effects of various coefficients of the PI controller on reactive component of the SSC.

According to Fig. 5, increasing these coefficients leads to the improvement of the reactive power sharing in the proposed controller as \( Q/Q^* \) gets closer to the unit value. The phase diagrams confirm the improvement process as depicted in Fig. 6.

IV. RESULTS AND DISCUSSIONS

The proposed model in Fig. 7 has been simulated in Matlab/Simulink environment and performance of the SSC is evaluated under different operating conditions. Simultaneous changes of low-value inertia and virtual mechanical power error are considered to ensure the dynamic stability of the SSC under load changes and inversed power flow. The system parameters can be found in Table I.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>dc-link Voltage (( v_{dc} ))</td>
<td>850 V</td>
<td>( J_1 )</td>
<td>8e-8 s</td>
</tr>
<tr>
<td>Phase ac voltage</td>
<td>220 V</td>
<td>( P_m )</td>
<td>3888.9 W</td>
</tr>
<tr>
<td>Fundamental frequency</td>
<td>50 Hz</td>
<td>( P )</td>
<td>3.5 kW</td>
</tr>
<tr>
<td>Switching frequency</td>
<td>10 kHz</td>
<td>( Q )</td>
<td>2.5 kVAR</td>
</tr>
<tr>
<td>REIC resistance</td>
<td>0.1 ( \Omega )</td>
<td>REIC inductance</td>
<td>43 mH</td>
</tr>
</tbody>
</table>

Fig. 7. General structure of the proposed model with simultaneous variation of inertia and VMP error.
The dynamic evaluation of the SSC under a disconnection of RER penetration is discussed in this sub-section. A disconnection of RER power of 4.5kW+j2.5kVar is occurred in the PCC at t=0.1s. Then, after this condition, the SSC-based REIC and PMSG start to provide active and reactive power needed for power grid stability at t=0.25s. Fig. 8 illustrates the active and reactive power of SSC-based RER, voltage magnitude and frequency of grid with the existence of SSC-based RER under RER penetration disconnection operating condition. In this evaluation, the simultaneous changes of low-value inertia and virtual mechanical power error are considered for proposed SSC. The scenario of such a condition is taken into account when the RER penetration disconnection takes place at t=0.1 and the SSC-based RER and PMSG doesn’t immediately operate. After experiencing the effects of the disconnection, SSC-based RER and PMSG woks at t=0.25. With the first values of \((\Delta P_{m1}, J_{1})\) shown as blue color, all variable states of SSC-based RER and power grid have their best operation of steady state and dynamic responses as depicted in Fig.8. The worst case is belongs to purple one for \((\Delta P_{m1}, J_{1})\) as shown in Fig.8.

![Fig. 8. RER active and reactive power, voltage magnitude and frequency with simultaneous changes of low-value inertia and virtual mechanical power error \((\Delta P_{m1}, J_{1})\)(\(\Delta P_{m2}, J_{2}\))(\(\Delta P_{m3}, J_{3}\))(\(\Delta P_{m4}, J_{4}\)) during load changes.](image)

V. CONCLUSION

A single synchronous controller (SSC) has been proposed in this paper for the control of interfaced converters for integration of large-scale renewable energy resources (RERs) into the power grid. All the features of a SG i.e., inertia and virtual mechanical power (VMP) error are considered in the structure of the SSC in order to simulate the behavior of SG in the operation of interfaced converters and provide a stable operation for the power grid under high penetration of RER.

An active and reactive power-based dynamic model has been developed and, based on it, two closed-loop control diagrams were shaped in order to analyze the stability of the power grid under different values of characteristics of SG, employed in the SSC. The presented results confirmed that by application of the proposed SSC, the power grid can operate in a stable operating condition under the penetration of large-scale RERs through the power electronic converters.

REFERENCES